

Higher Maths
Unit 3 Specimen NAB
Number 2

Outcome 1

1. The points P, Q, and R have coordinates $(2, -3, 3)$, $(6, -2, 0)$, $(14, 0, -6)$ respectively.

(a) Write down the components of \overrightarrow{PQ}

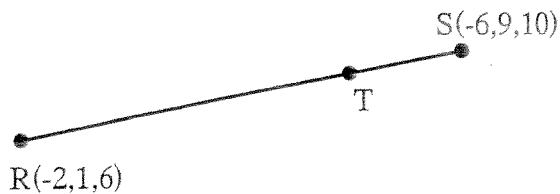
1

(b) Hence show that the points P, Q, and R are collinear.

3

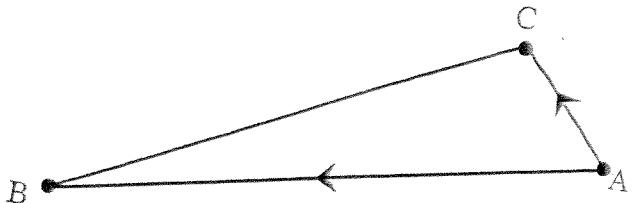
2. The point T divides \overrightarrow{RS} in the ratio 3:1, as shown in the diagram.
 Find the coordinates of T.

3



3. The diagram shows vectors \overrightarrow{AB} and \overrightarrow{AC} where

$$\overrightarrow{AB} = \begin{pmatrix} 5 \\ 0 \\ 12 \end{pmatrix} \quad \text{and} \quad \overrightarrow{AC} = \begin{pmatrix} 2 \\ -2 \\ 1 \end{pmatrix}$$



(a) Find the value of $\overrightarrow{AB} \cdot \overrightarrow{AC}$

1

(b) Hence find the size of angle BAC.

4

Outcome 2

4. (a) Given $y = \frac{1}{3} \sin x$, find $\frac{dy}{dx}$. 1
- (b) Differentiate $-6\cos x$, with respect to x. 1
5. Given $g(x) = (x - 1)^6$ find $g'(x)$. 2
6. (i) Find $\int 2 \sin x dx$.
- (ii) Integrate $\frac{1}{2} \cos x$, with respect to x. 3
7. Evaluate $\int_1^2 (x + 3)^4 dx$ 4

Outcome 3

8. (a) Simplify $\log_b 8 + \log_b 5$ 1
- (b) Simplify $5 \log_9 3 - \log_9 27$ 4
9. Solve $e^x = 5.7$ 2
10. Solve $\log_3(x + 1) = 2$ 2

Outcome 4

11. Express $4 \cos x^\circ + \sin x^\circ$ in the form $k \cos(x - \alpha)^\circ$ where $k > 0$ and $0 \leq \alpha < 360$. 5